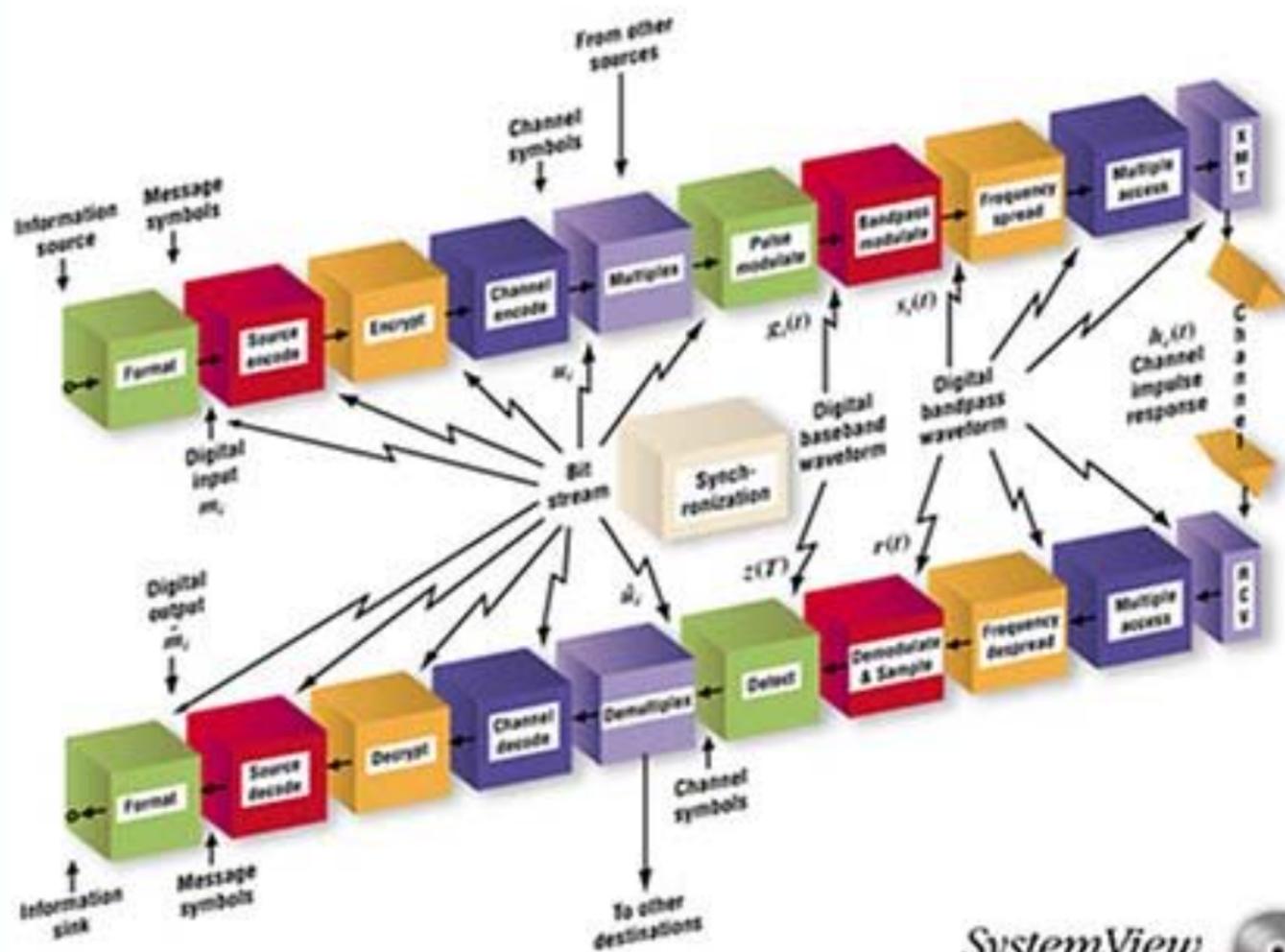


Digital

SECOND EDITION

Communications

Fundamentals and Applications



BERNARD SKLAR

DIGITAL COMMUNICATIONS

Fundamentals and Applications

Second Edition

BERNARD SKLAR

*Communications Engineering Services, Tarzana, California
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